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Bubble entrainment by a sphere falling through a horizontal soap foam

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PACS 47.57.Bc – Foams and emulsions

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Abstract – Processes such as particle separation, froth flotation and explosion suppression rely on the extent to which particles are trapped by foam films. We simulate the quasi-static motion of a spherical particle through a stable, horizontal soap film. The soap film subtends a fixed contact angle, in the range $10 - 135^\circ$, where it meets the particle. The tension and pressure forces acting on the particle are calculated in two cases: when the film is held within a vertical cylinder, trapping a bubble but otherwise free to move vertically, and when the outer rim of the film is held in a fixed circular wire frame. Film deformation is greater in the second case, and the duration of the interaction therefore increases, increasing the contact time between particle and film. As the soap film returns towards its equilibrium shape following the passage of the particle a small bubble is trapped for contact angles below a threshold value of 90° . We quantify how the size of this bubble increases when the particle is larger and when the contact angle is smaller.

Introduction. – Aqueous foams interact with particles in a number of important situations [1, 2]; at high particle density the particles can even replace surfactant and stabilise the foam [3]. At the other extreme, foam films can be used to separate individual particles based on their size [4]. In between, processes such as froth flotation and explosion suppression [2, 5] rely on the extent to which particles are trapped by foam films. Once in the film, particles may rotate and, depending on parameters such as the contact angle, may cause rupture [6].

Le Goff et al. [7] found that small millimetric-sized particles falling on to a soap film at speeds of about 1 m/s do not break the film. That is, after the particle has passed through the soap film the film “heals” itself [8]. This arrangement of a stable soap film held horizontally while a small spherical particle falls onto it permits an investigation of the forces that the soap film exerts on the particle and the consequent changes to the particle’s velocity. The soap film can be considered to represent one repeating unit of a more extensive “bamboo” foam [9], in which successive impacts between the particle and different soap films could bring the particle to rest, representing a microscopic approach to the way in which a foam can be used in impact protection [5]. In the following, we choose the particle’s weight sufficiently large that it is never trapped by a sin-

gle soap film. Then the film is pulled into a catenoid-like shape as it is stretched by the particle, until, similar to the usual catenoid instability [10], the neck collapses and the soap film returns to its horizontal state.

We will show that the forces exerted on the particle depend strongly on the contact angle along the triple line (Plateau border) where the liquid, gas and solid particle meet. In an experiment this contact angle could be adjusted by coating the particle [11]. We allow the contact angle at which the soap film meets the spherical particle to vary: the equilibrium case is a contact angle of $\theta_c = 90^\circ$ [12], in which the sphere is assumed to be coated with a wetting film that allows the soap film to move freely. However, experimental photographs [7, 13] show that the soap film wraps around the particle, with a contact angle far from 90° , before forming a catenoid-like neck. This suggests that the particle’s motion is faster than the mechanical relaxation of the foam. Here we nonetheless employ quasistatic simulations, and presume that the only effect of the dynamic nature of the experiments is to adjust the contact angle between particle and film. We consider several values of θ_c down to 10° .

In experiments, the collapse of the catenoidal neck above the particle generates a small bubble [7], as for the impact of a liquid drop on a liquid surface [14, 15] and the

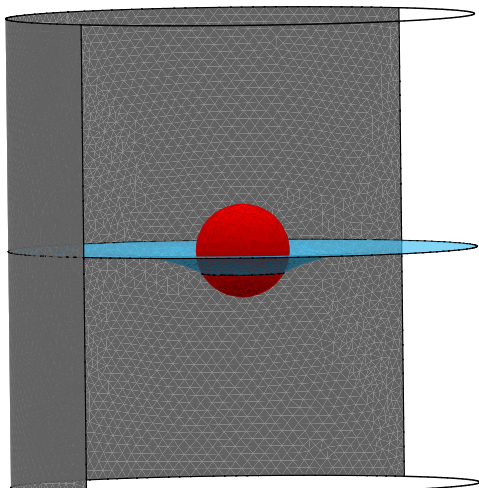


Fig. 1: A spherical particle passing through a soap film held in a cylinder. The contact angle between the particle and the film is 30° in this example.

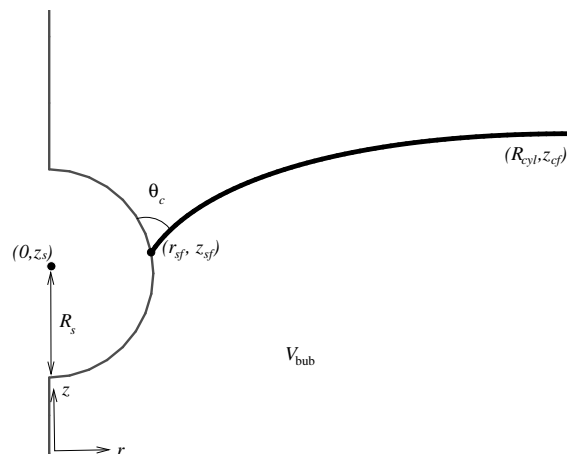


Fig. 2: The axisymmetric structure under consideration, shown in the (r, z) plane. In case 1 there is a bubble of fixed volume V_{bub} and the vertex at position (R_{cyl}, z_{cf}) is free to move, while in case 2 there is no volume constraint and the vertex is fixed.

51 collapse of an isolated soap-film catenoid [16]. This small
 52 bubble was not seen in previous simulations with a 90°
 53 contact angle [9, 12]. Our new simulations make clear why
 54 this is the case: only with a contact angle smaller than 90°
 55 does the film curve around the particle sufficiently before
 56 detachment to enclose such a volume of gas.

57 The particle in our simulations, described below, is a
 58 sphere of radius R_s and mass m grams, and hence with
 59 density $\rho = m/(4/3\pi R_s^3)$; see figure 1. It falls towards a
 60 film with interfacial tension γ (so a film tension of 2γ).
 61 We consider two cases:

- 62 1. the soap film is held in a cylinder of radius R_{cyl} and
 63 height $H = 2R_{\text{cyl}}$. The film encloses a bubble of fixed
 64 volume $0.5H\pi R_{\text{cyl}}^2$, i.e. that fills the lower half of the
 65 cylinder. In this case both the tension in the film and
 66 the pressure in the bubble exert a force on the sphere
 67 once it touches the film.
- 68 2. the soap film is held by a fixed ring of radius R_{cyl} . In
 69 this case only the tension in the film exerts a force on
 70 the sphere.

71 The Bond Number is defined as $Bo = \frac{1}{2}\rho g R_s^2 / \gamma$. In the
 72 simulations we ensure that the Bond number is just greater
 73 than one, indicating that gravitational forces should ex-
 74 ceed the retarding force due to surface tension. Making
 75 the density (and hence the Bond number) smaller would
 76 lead to the sphere being trapped by the film. **In-
 77 creasing the particle density would mean that the quasistatic ap-
 78 proximation that we employ would be less appropriate;
 79 indeed, balancing capillary effects with inertial effects for
 80 the particles that we consider below, by choosing a Weber
 81 number of one, suggests that particle velocities should be
 82 at most 1 m/s for this approximation to be valid.**

83 **Method.** –

Geometry. We use the Surface Evolver [17] to com- 84
 85 pute the shape of the soap film. Since this software gives
 86 information about static situations, we **treat the motion as**
 87 **overdamped**, and therefore the sphere and soap film move
 88 through a sequence of equilibrium positions determined by
 89 the forces acting.

By symmetry the sphere must remain in the centre of 90
 91 the film, so we perform an axisymmetric calculation in the
 92 (r, z) plane (figure 2). The film is represented by a curve
 93 whose endpoints touch, respectively, the sphere (or the
 94 axis of the cylinder before attachment and after detach-
 95 ment) and the outer cylinder / ring. We discretize the
 96 curve into short straight segments of length dl and write
 97 the energy of the system as

$$E_{\text{film}} = 2\gamma \sum_{\text{segments}} 2\pi r dl. \quad (1)$$

We restrict segments to have lengths in the range **0.01 –** 98
 99 **$-0.05R_{\text{cyl}}$** which balances the need for accuracy with a
 100 short computational time.

To include a contact angle θ_c we add a further term to 101
 102 the energy representing a spherical cap of film with tension
 103 $2\gamma \cos \theta_c$ that covers the lower part of the sphere. This is
 104 based on the height z_{sf} of the film where it meets the
 105 sphere:

$$E_{\theta_c} = 2\gamma \cos \theta_c \cdot 2\pi R_s (z_{sf} - (z_s - R_s)), \quad (2)$$

where z_s is the height of the centre of the sphere. This 106
 107 energy is set to zero before attachment and after detach-
 108 ment.

In case 1 we must also account for the volume V_{bub} of the 109
 110 bubble trapped beneath the soap film. We calculate this
 111 volume based on the shape of the film and the positions
 112 of its endpoints. There are three terms required:

$$V_1 = \sum_{\text{segments}} \pi r^2 dz$$

$$V_2 = \begin{cases} 0 & z_{sf} < z_s - R_s \\ \pi R_s^2 (z_{sf} - z_s + \frac{2}{3} R_s) - \frac{\pi}{3} (z_{sf} - z_s)^3 & z_s - R_s \leq z_{sf} \leq z_s + R_s \\ \frac{4}{3} \pi R_s^3 & z_{sf} > z_s + R_s \end{cases} \quad (3)$$

$$V_3 = \pi R_{\text{cyl}}^2 z_{cf},$$

113 with $V_{\text{bub}} = V_3 - V_2 - V_1$. The first term (V_1) is the vol-
 114 ume of revolution about the z axis of the film between its
 115 endpoints, and the second term (V_2) is the volume of the
 116 spherical cap below the the point of contact between the
 117 film and the sphere. These are both subtracted from the
 118 third term (V_3), which is the total cylindrical volume en-
 119 closed by the outer wall of the cylinder beneath the point
 120 of contact z_{cf} between the film and the cylinder wall.

121 *Forces.* We consider two forces in addition to the
 122 weight mg acting in the negative z direction. The ten-
 123 sion force F_γ is due to the pull of the soap film around
 124 its circular line of contact with the sphere and the pres-
 125 sure force F_p , which is only relevant in case 1, is due to
 126 the pressure p_{bub} in the trapped bubble which acts over
 127 the surface of the sphere below the contact line. We are
 128 interested only in the vertical component of these forces,
 129 since by symmetry the other components cancel.

130 We define the angle θ that the film subtends with the
 131 centre of the sphere, $\tan \theta = (z_{sf} - z_s)/r_{sf}$, and then the
 132 z -components of the forces are

$$F_\gamma = 2\gamma \cdot 2\pi r_{sf} \cos(\theta - \theta_c) \quad (4)$$

133 and

$$F_p = \pi r_{sf}^2 p_{\text{bub}}. \quad (5)$$

134 *Motion.* We perform a quasi-static simulation in
 135 which the position of the sphere is held fixed while the
 136 equilibrium shape of the film is found, and then the sphere
 137 is moved a small distance in the direction of the resultant
 138 force. In case 1 the bubble pressure is found from the
 139 Lagrange multiplier of the volume constraint, eq. (3).

140 We start the simulation with the sphere just above a
 141 horizontal film, and move the sphere downwards until con-
 142 tact is made and the inner end of the film jumps to a new
 143 position on the sphere. Then the change in the vertical
 144 position of the sphere is determined by the net force acting
 145 on it:

$$\Delta z_s = \epsilon (F_\gamma + F_p - mg), \quad (6)$$

146 where the small parameter ϵ , which we think of as the
 147 inverse of a viscosity, is taken equal to 1×10^{-5} (which
 148 we find is sufficiently small not to change the results).

149 Detachment occurs when the film nears the top of the
 150 sphere and becomes unstable, at which point it jumps
 151 back to being horizontal, and we then end the simulation. Note
 152 that Δz_s is always negative in our simulations, since the
 153 weight of the sphere is large enough that it always exceeds
 154 the tension force.

155 **Results.** – The simulations are performed in cgs
 156 units, with $R_{\text{cyl}} = 1\text{cm}$ and interfacial tension $\gamma =$

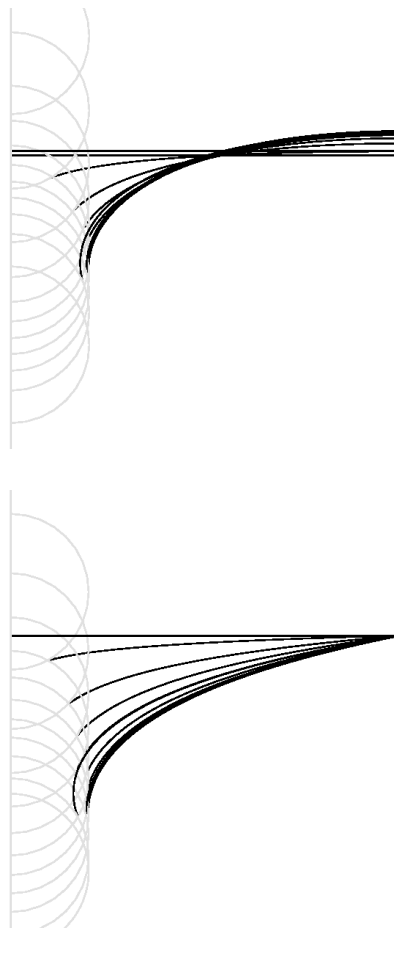
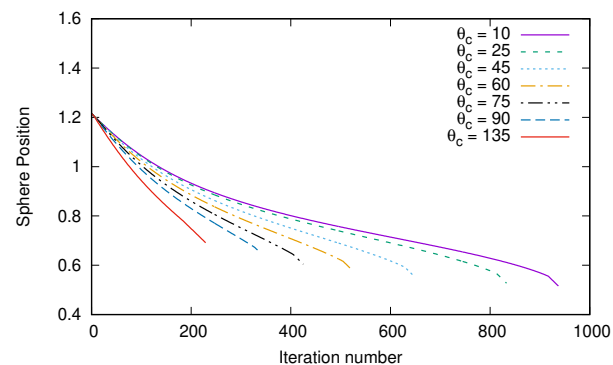


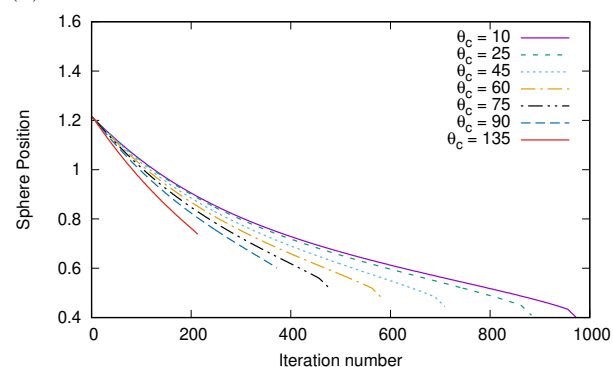
Fig. 3: Film shapes recorded as the sphere descends, with contact angle $\theta_c = 10^\circ$, shown every 100 iterations. (a) Case 1, where a wetting film on the outer cylinder wall allows the film to slip there and hence meet the wall at 90° . (b) Case 2, where the film is fixed at the outer cylinder wall. In each case, the film exhibits the greatest curvature just before detachment, and in the last sphere position shown the film has detached and returns to being horizontal.

157 30mN/m. We first consider a sphere of radius $R_s =$
 158 $0.2R_{\text{cyl}}$ and mass $m = 0.1$ grams. Then the particle den-
 159 sity is $\rho \approx 3\text{g/cm}^3$ and the Bond number is $Bo \approx 2$. An
 160 example of the shape of the film at different times is shown
 161 in figure 3. See the supplementary material for videos of
 162 the motion.

163 *Sphere position, soap film area, and point of contact.*
 164 The vertical position of the centre of the sphere is shown
 165 in figure 4. Following attachment we observe a shallower
 166 curve for smaller contact angles, indicating that the forces
 167 retard the motion of the sphere to a greater extent when
 168 the contact angle is small. When the contact angle is
 169 larger, for example with θ_c greater than about 45° , the
 170 sphere motion is at first accelerated, as the film pulls it
 171 downwards. In case 1, the bubble pressure is also negative
 172 at first (see figure 8 below), adding to this effect. For the

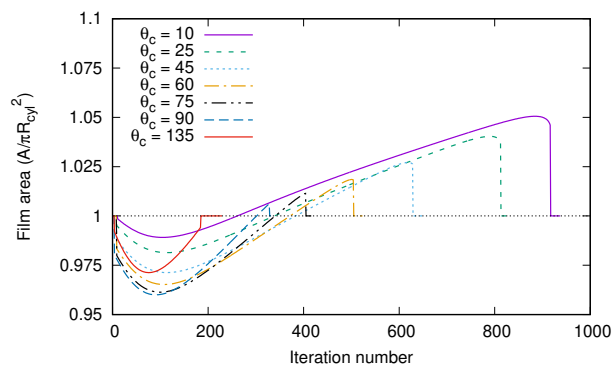


(a)

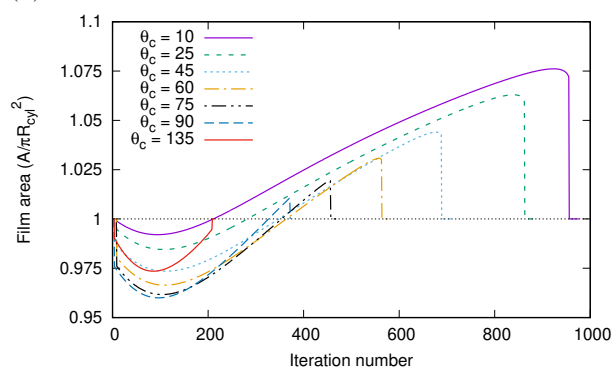


(b)

Fig. 4: The height of the centre of the sphere under the action of its weight and the forces that the foam exerts on it. The horizontal axis corresponds to time, in units of ϵ . (a) Case 1. (b) Case 2.



(a)



(b)

Fig. 5: The area of the soap film as the sphere passes through it. (a) Case 1. (b) Case 2.

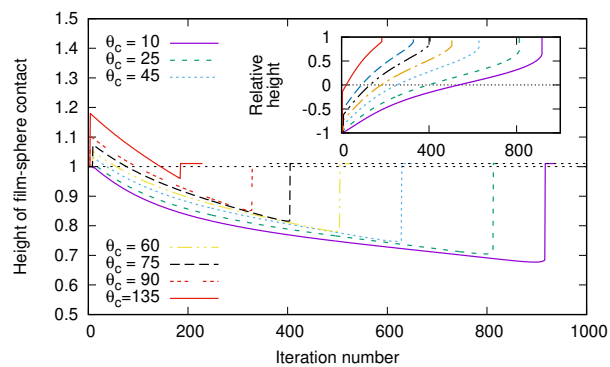
173 contact angle of $\theta_c = 135^\circ$ this significantly reduces the
 174 time of interaction before the film detaches from the top
 175 of the sphere.

176 When the sphere first meets the film the film area is
 177 reduced (figure 5) because it contains a circular hole that
 178 is filled by the sphere. As the sphere descends further,
 179 the film deforms in order to obey the volume constraint
 180 (in case 1) or the fixed rim at the cylinder wall (in case
 181 2) and to satisfy the contact angle where they meet. This
 182 causes the film area to increase, until the film approaches
 183 the point of detachment. For **contact angles above 90°**
 184 **(for example $\theta_c = 135^\circ$) the area of the film never ex-**
 185 **ceeds** its equilibrium value, $A = \pi R_{\text{cyl}}^2$, indicating that
 186 it is not greatly deformed and that detachment occurs
 187 quickly. Comparing case 1 to case 2, for all other contact
 188 angles simulated, the film is slightly more deformed when
 189 its outer rim is fixed (case 2).

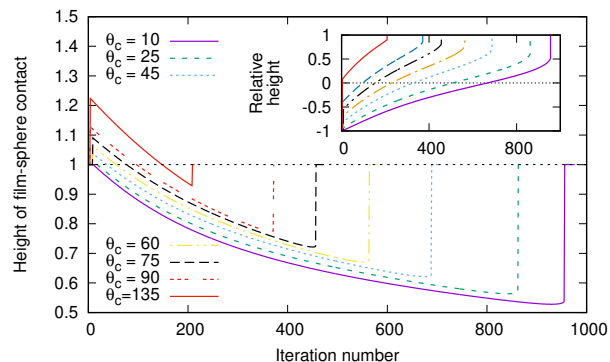
190 There is a jump in the vertical position of the circular
 191 line of contact when the film first meets the sphere
 192 (figure 6). The contact line rises to a new position to sat-
 193 isfy the contact angle (without, in case 1, violating the
 194 volume constraint), to a degree that increases with the
 195 contact angle. This end of the film is then pulled down
 196 by the sphere, more so for large contact angles, and the
 197 decrease is monotonic.

198 Detachment occurs *before* the inner end of the soap film
 199 reaches the top of the sphere. Instead, there is a sort of
 200 “pre-emptive” instability [18]: the curved soap film be-
 201 comes unstable, the line of contact jumps upwards, and a
 202 new configuration consisting of a flat film above the sphere
 203 is reached. This is seen, for example, in the abrupt jump
 204 in the surface area of the film, shown in figure 5, at the
 205 point of detachment. Fixing the outer rim of the film (case
 206 2) leads to a greater deformation of the film (figure 5) and
 207 hence to the film becoming unstable when the line of con-
 208 tact is further from the top of the sphere (figure 6 insets).
 209 In case 1, the film returns to a higher position after the
 210 sphere has passed, because the volume enclosed beneath
 211 the film is augmented by the volume of the sphere. In
 212 case 2, without a volume constraint, the interaction time
 213 (when the film and sphere are in contact) is longer for each
 214 value of contact angle compared to case 1, and the sphere
 215 descends further before detachment. Hence the overall ef-
 216 fect of constraining the volume rather than the outer rim
 217 of the film is to retard the sphere.

218 In case 1 the outer rim of the film, where it touches
 219 the cylinder wall, behaves slightly differently (data not
 220 shown). It at first drops suddenly, i.e. in the opposite
 221 sense to the inner contact line, and then increases until
 222 the inner contact line approaches the top of the sphere.
 223 It then descends again before suddenly returning to the
 224 same vertical position as the inner contact line when the

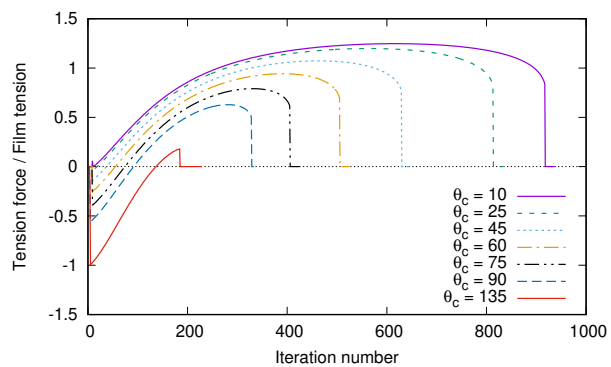


(a)

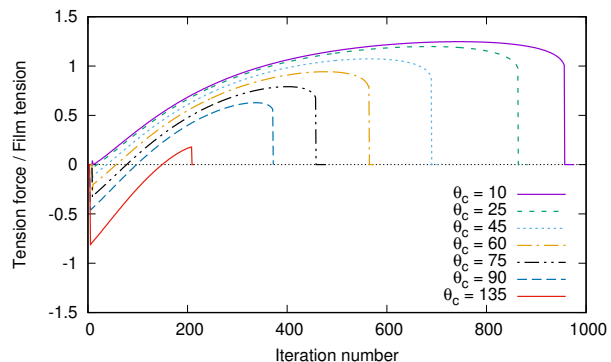


(b)

Fig. 6: The vertical position z_{sf} of the line where the film touches the sphere. The inset shows this position relative to the height of the centre of the sphere, $(z_{sf} - z_s)/R_s$. (a) Case 1. (b) Case 2.



(a)



(b)

Fig. 7: Tension forces exerted on the sphere, determined by the direction in which the film pulls multiplied by its tension. (a) Case 1. (b) Case 2.

225 film detaches and becomes flat.

226 *Measured forces.* We show the forces acting on the
 227 sphere in figures 7 and 8. For large contact angles the
 228 film pulls the sphere downwards, accelerating its motion.
 229 The opposite occurs for small contact angles, and so the
 230 time over which the sphere contacts the sphere is extended.
 231 Just before the abrupt drop in force at the point of detach-
 232 ment, there is a slight reduction in the tension force as the
 233 perimeter of the contact line becomes small, ameliorating
 234 the pull from the film.

235 In case 1, the pressure in the bubble can be either posi-
 236 tive or negative, depending on the curvature of the film.
 237 The pressure force on the sphere is determined by this
 238 pressure multiplied by the vertically-projected area of the
 239 sphere over which the bubble touches the sphere, eq. (5).
 240 The pressure force is much smaller in magnitude than the
 241 tension force. For the contact angle of 135° the bubble
 242 pressure is large and negative for much of the passage of
 243 the sphere, because of the curvature induced by the con-
 244 tact angle, so in this case the pressure force “sucks” the
 245 sphere downwards and detachment occurs earlier than in
 246 case 2.

247 For smaller contact angles, for example $\theta_c = 10^\circ$, the
 248 pressure is always positive, opposing the downward motion
 249 of the sphere. Yet it is still the case that detachment

250 occurs sooner in case 1, even though for a given contact
 251 position the tension force is similar in both cases. Further,
 252 the film becomes unstable at a lower position in case 2.
 253 The resolution of this apparent paradox is that when the
 254 contact line is at a certain position on the sphere, the
 255 sphere is at a different height in the two cases, because
 256 of the need to satisfy the different constraints and for the
 257 film to meet the sphere at the same contact angle. In
 258 particular, before the contact line passes the equator of
 259 the sphere ($z_{sf} < z_s$), it moves around the sphere more
 260 slowly in case 2, while above the equator it moves more
 261 quickly (but over a shorter distance).

262 *Bubble entrainment.* Although our quasistatic simu-
 263 lations do not resolve the rapid film motion during detach-
 264 ment, we can gain an idea of the size of the small bubble
 265 that is trapped [7] by examining the shape of the soap film
 266 immediately before detachment, as shown in figure 9. **Our**
 267 **idea is that the inner part of the film rotates rapidly to-**
 268 **wards the vertical axis of the cylinder during detachment,**
 269 **and that the shaded region doesn’t change its shape dur-**
 270 **ing this motion. Then, when the film touches the axis**
 271 **part-way along its length, this volume of gas is trapped.**
 272 We calculate the area of the region in the (r, z) plane that
 273 is shaded in the figure, between the soap film and a
 274 radial line through the point of the soap film closest to the
 275 vertical axis. This is likely to be an underestimate as the

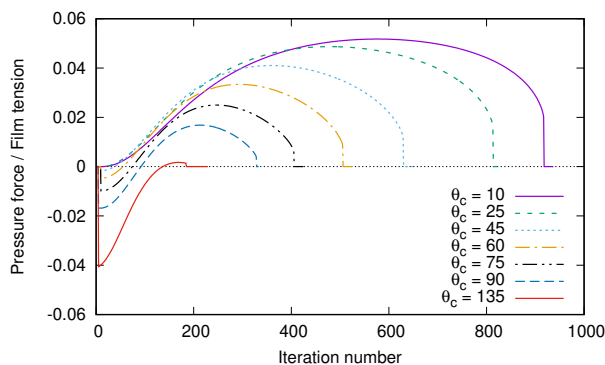


Fig. 8: Pressure forces exerted on the sphere in Case 1.

276 curvature of the film around the catenoidal neck is likely
277 to increase during detachment.

278 Figure 9 shows that for small contact angles the bubble
279 size can reach almost 0.01cm^3 . The limit in which the
280 contact angle tends to zero appears to give a well-defined
281 value for the maximum size of this small satellite bubble.
282 For contact angles of 90° and above there is no bubble
283 because the point on the soap film nearest to the vertical
284 axis is where the film touches the particle.

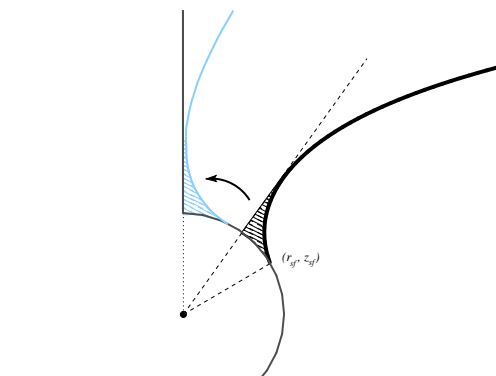
285 There is a small effect of the choice of boundary con-
286 ditions: in case 2, without a pressure force, the bubble
287 is about 30% larger for $\theta = 10^\circ$ (although this difference
288 decreases as the contact angle increases). This is because,
289 as noted above, in case 2 the instability that causes the
290 film to detach occurs earlier, when the line of contact is
291 closer to the equator of the sphere.

292 In case 1 with a fixed contact angle of 10° we varied the
293 size of the spherical particle and again estimated the size
294 of the trapped bubble. For a sphere of a given radius, we
295 must choose between a fixed particle mass (weight) or a
296 fixed particle density.

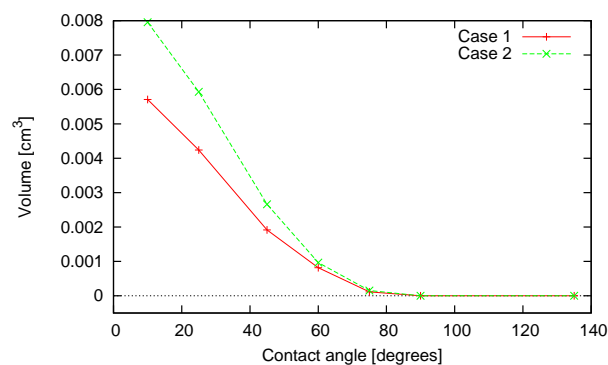
297 In the former case, the tension force opposing the de-
298 scent of the particle increases with particle radius, but
299 since the sphere does not increase in weight, it is brought
300 to rest by the soap film once the particle exceeds a critical
301 radius. The maximum vertical tension force that the soap
302 film could exert on the sphere to counteract its weight oc-
303 curs when the film meets the sphere on its equator and
304 pulls vertically upwards; then the film tension multiplied
305 by the sphere circumference is $4\pi\gamma R_s$. So the critical
306 radius is $R_{s(m)} \approx mg/(4\pi\gamma)$. With $m = 0.12\text{g}$ this is
307 $R_{s(m)} \approx 0.31\text{cm}$.

308 In the latter case, only when the particle falls below a
309 critical radius is it brought to rest by the soap film, $R_{s(\rho)} \approx$
310 $\sqrt{3\gamma/(\rho g)}$. With $\rho = 6\text{g/cm}^3$ this is $R_{s(\rho)} \approx 0.12\text{cm}$.

311 Figure 10 shows that the size of the bubble that is
312 trapped is the same in both cases. So it is determined
313 by the shape of the soap film only, which in turn arises
314 from the film meeting the sphere, of whatever radius, at
315 the given contact angle. Therefore the size of the trapped
316 bubble increases with sphere size, since the film is more
317 greatly deformed when the sphere is larger. This also val-



(a)



(b)

Fig. 9: (a) Close to the contact line between the soap film
and the sphere, at the last iteration before detachment (dark
shading), we calculate the shaded volume to estimate the vol-
ume of the small bubble that would be left behind if this region
moved uniformly toward the axis (light shading). (b) The bub-
ble volume depends strongly on the contact angle, depends only
weakly on whether we consider case 1 or case 2, and vanishes
for contact angles greater than 90° .

318 idates that our choice of ϵ is sufficiently small that the
319 numerical method works even if, for heavy particles, the
320 sphere descends quickly.

321 There is also a small dependence of the size of the
322 trapped bubble on the cylinder size. As the cylinder be-
323 comes larger, the sphere descends further before detach-
324 ment, and so greater film deformation is possible. In ad-
325 dition, the pressure force is reduced in a larger cylinder,
326 so the result should be closer to case 2. Thus, the trapped
327 bubble is slightly larger if the cylinder radius is larger.

328 To validate our predictions, we compare with the image
329 in Figure 1 of [7], which shows a sphere of radius 0.16cm
330 falling through a soap film trapping a bubble. (The cylin-
331 der radius and sphere mass are not recorded.) The bub-
332 ble is trapped against the upper part of the sphere, but
333 appears to be roughly hemispherical with radius 0.08cm ,
334 and hence a volume of 0.001cm^3 . The data point, shown
335 in figure 10, lies close to our prediction.

336 **Conclusions.** — We have explained the effect of con-
337 tact angle on the forces that act on a spherical particle
338 passing through a soap film. The duration of the interac-

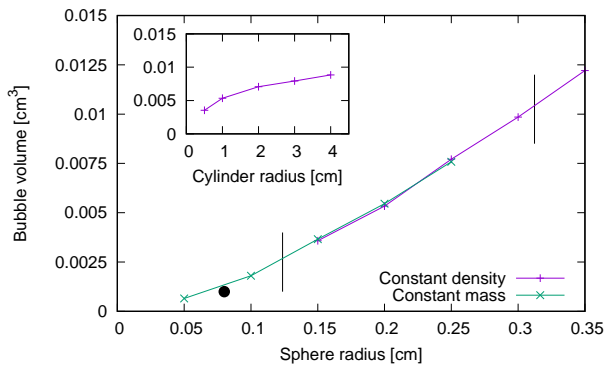


Fig. 10: With contact angle $\theta_c = 10^\circ$ in case 1, the volume of the bubble that is trapped by the film increases with the size of the particle and (inset) depends weakly on the size of the cylinder containing the soap film. **The solid circle is experimental data [7]. With fixed mass only spheres with radius up to $R_{s(m)}$ pass through the film; with constant density only spheres with radius larger than $R_{s(\rho)}$ pass through the film; these bounds are indicated by the vertical lines. The size of the trapped bubble is the same in both cases, indicating that it is determined by the geometry of the soap film.**

tion is determined by the contact angle and also the way in which the film is deformed; for example, with low contact angles the particle moves more slowly, and stays in contact with the soap film for longer. Further, the interaction depends upon the details of the experiment: greater deformation is induced by holding the film in a fixed circular wire frame than in a cylindrical tube, where it traps a bubble but where the outer circumference of the film is not fixed, such as in a soap-film meter [13]. In the latter case there is an additional force on the particle due to the pressure in the bubble, but this is negligible in determining the dynamics of the system.

Analysing the shape of the soap film just before detachment allows us to predict the size of the small bubble that is formed when a particle passes through a film. The entrainment of this air and the formation of interface could play a role in determining the efficacy of using foams for the suppression of explosions. We find that the bubble increases in size as the particle gets larger, and can exceed 10mm^3 .

Extending our predictions to more general cases, such as oblique impact and non-spherical particles [6, 12], will require more computationally-intensive three-dimensional simulations.

* * *

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